For an $\ell$-unital $\ell$-ring $R$, various recognition criteria are given for $R$ to be isomorphic to a matrix $\ell$-ring over an $\ell$-unital $\ell$-ring with the entrywise order.